## UDL Lesson Plan Template

Instructor: $\qquad$ Janie Shafer
Learning Domain: Geometry Grade: 9 and10

Lesson Objective/s: The student will identify the relationship between two lines, classify angles formed by two lines and a transversal, and find angle measurement. The student will determine the relationship between angles formed by two parallel lines and a transversal.
Assessment/s: Pre-Test, post-test, Group discussion , Peer discussion, Homework Assignment, Closure activity, Chapter Test with Alternate Assessment project
State Standards Correlation: M.2HS.STP. 4 Students will prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent.

UDL Applications Key: Representation Engagement Expression
Pre-planning Activities: Objectives and class agenda posted on board, prepare new vocabulary words and add symbols/example/visualization, determine how students will be paired and grouped, protractors, graphing calculators, reference books and computers with internet access, scavenger hunt directions, pre and post test run off, map of D.C. ,colored markers, masking tape, $3 \times 5$ index cards

| Lesson Element | Procedures | Time | What is the teacher doing? | What are the students doing? | Materials |
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| $\begin{gathered} \text { Lesson Setup } \\ \& \\ \text { Lesson Opening } \end{gathered}$ | Objectives and class agenda posted on board before students enter class. Warm up: Pre-test-The student will identify what are parallel lines, what is coplanar, types of angles formed by 2 interesting lines cut by a transversal, and the relationship between the angle measurements. <br> Your score on the pre-test will not hurt your class grade. It is just an indicator for me, so that I know what I need to teach and reinforce. As always, do your best. <br> Lesson Opener: Ask students: 1. Have you ever been to Washington D.C. <br> 2. Have you ever been lost in a city? 3. Do you know who Pierre Charles <br> L'Enfant was? <br> (May want to use a more local map, area that more students should be familiar with. Suggested on the Lesson Plan Critique.) | 5 min . <br> 3 min. | Pass out pre-test. <br> Lead <br> discussion <br> on <br> questions 1- <br> 3 | Listen to directions and take pre-test <br> Participate in discussion of questions 1-3. | Copy of pre-test for each student. <br> Extra <br> pencils. <br> Computer, electronic white board with projector, partial map of streets in Washington D.C. (Map created by Pierre Charles L'Enfant. |
| Lesson Body | Show enlarged partial map of streets in Washington D.C. on the smart | 5 min | Instructin | Study map, | Individua |

board. Tell the students that each street is part of a line or is a line segment. These lines all lie on the same flat surface or plane. Ask students to work with a partner and answer the following:

1. Two lines are coplanar if they lie in the same plane. What different relationships can occur between two coplanar lines?
2. Do parallel lines have to lie in the same plane?
3. Use the map to give an example of each relationship you described in number 1.
4. Two lines are parallel lines if they are coplanar and do not intersect. Identify 2 pairs of lines formed by the streets that appear to be parallel.
Assessment - Ask the following questions to verify student understanding. 1. Name several planes in our classroom. 2. What does it mean to be coplanar? 3. Locate parallel lines in our classroom. 4. Do parallel lines have to be coplanar?

Introduce the student to angles that are formed when lines are cut by a transversal. Show a drawing of 2 lines, labeled line $m$ and $n$ (not parallel and a third line (line $t$ ) intersecting the first two. (They can refer to the map and use $6^{\text {th }}$ Street and New Jersey Avenue as the first two lines, and New York Avenue as the street that intersects the other two.) Tell the students line $t$ is called the transversal of lines $m$ and $n$. When a line intersects two or more other lines all at different points, the line is called a transversal.
Ask the students, how many angles are created when two lines are cut by a transversal.

Show 2 nonparallel lines $p$ and $q$ cut by a transversal $r$. (Can use Rhode Island Ave as line p, Massachusetts Ave. as line q, and $9^{\text {th }}$ Street as the transversal r). Tell students four of the eight angles formed are interior angles and 4 are exterior. Ask the students to identify which are interior

|  | g, leading class discussion Pose questions to assure understan ding and a form of assessmen t | collaborate with partner, give examples, answer questions | 1 copy of map of D.C. Copy of map on white board. All other illustratio ns on white board |
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| 5 min . | Teacher will show drawing of parallel lines cut by transvers al. | Observe drawing or use map and conclude there are 8 angles. | Drawing of 2 <br> intersecti ng lines cut by a transvers al |
| 10 min. | Draw <br> illustratio <br> $n$ of parallel | Identify different types of | Drawing of 2 intersecti ng lines |

and explain why. Ask students to identify which are exterior and explain why. We are going to learn about other ways to classify these angles.
Explain that 2 angles are alternate interior angles if they lie between the 2 lines on opposite (alternate) sides of the transversal. Ask students to identify both pairs of alternate interior angles. Two angles are alternate exterior angles if they lie outside the two lines on opposite (alternate) sides of the transversal. Ask students to identify both pairs of alternate exterior angles.
Explain two angles are corresponding angles if they are on the same side of the transversal in corresponding or the same position. Ask students to name all pairs of corresponding angles.
Explain two angles are same side interior angles (sometimes called consecutive interior angles), if they lie in between the two parallel lines and on the same side of the transversal. Also explain that same side exterior angles lie on the exterior of the $\mathbf{2}$ parallel lines and on the same side of the transversal.
Assessment: Have a student draw and label example of 2 non parallel lines cut by a transversal on the smart board. The student will call on another classmate to identify and label a pair of angles on the smart board. That student in will call on another classmate to identify another pair of angles on the smart board. Continue the exercise until all pairs of possible angles have been identified.

Guided Practice: Next, students will discover properties of angles formed by intersection of transversal and parallel lines. Students may work in small groups (pre-assigned). Ask the students to use the worksheet with the examples of parallel lines cut by a transversal or on the DC map, consider parallel streets $9^{\text {th }}$ Street and \& 7th and Rhode Island Avenue as the transversal. Use a protractor to measure all of the angles. Record your results on your drawings. After measuring all angles, complete the following:

1. Identify all congruent angles.

| 10 min | lines cut by transvers al. Define different angles that are formed. <br> Teacher calls on volunteer to start identificat ion of angles <br> Pass out protracto rs and workshee t with examples of parallel lines cut | angles <br> Students create drawing \& identify pairs of angles <br> Work in small groups, pre assigned. Measure angles and record results. | cut by a transvers al <br> Smart board \& markers <br> Workshee t with several pairs of parallel lines cut by a transvers al |
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|  | 2. 2. Identify all pairs of corresponding angles. What do you notice about each pair of angles? <br> 3. Identify all pairs of alternate interior angles. What do you notice about each pair of angles. <br> 4. Identify all pairs of alternate exterior angles. What do you notice about each pair of angles? <br> 5. Identify all pairs of same side interior angles. Are the angles equal in measure? Find the sum of their measures. <br> 6. Identify all pairs of same side exterior angles. Are the equal in measure? Find the sum of their measures. <br> Call the class back together to have the students discuss and present their work. <br> Discuss what they can conclude about the angles formed when a transversal cuts a pair of parallel line. <br> Discuss what they can conclude about the pairs of same-side interior angles and same-side exterior angles. |  | by a <br> transvers <br> al, <br> circulate <br> around <br> room <br> while <br> students <br> measure <br> angles <br> and <br> record <br> responses <br> to <br> questions <br> 1-6. <br> Teacher <br> leads <br> discussion <br> on <br> conclusio <br> ns from <br> guided <br> practice | Record responses to questions 1-6. <br> Students present results and give conclusions <br> Students participate in developing properties of angles formed by parallel lines cut by a transversal. |  |
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| Extended Practice | The students are given 2 parallel lines cut by a transversal. One of the 8 angles formed is given the measurement of $\mathbf{1 0 2}$ degrees. The student will find the measure of the other 7 angles using the conclusions from the guided practice. (No protractors) Students will work individually. | 5 min . | Circulate, monitor, and facilitate | Apply conclusions to specific problem | Worksheet with pair of parallel lines cut by a |


|  |  |  |  | transversal. <br> Given the <br> measureme <br> nt of one <br> angle. |  |
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| Lesson Closing | Assessment: Pass out a 3x5 index card to each student. Have them draw a <br> pair of parallel lines cut by a transversal. Number the angles formed from <br> 1 to 8. Identify 1 pair of angles and describe their relationship. Please hand <br> me the card as you leave class. | $\mathbf{2}$ min | Pass out <br> index cards <br> as Exit <br> Cards and <br> give the <br> directions | Students <br> complete Exit <br> cards | 3x5 Index <br> Cards |


| Possible Learner Barriers: | Possible Solutions |
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| Making connections to real life | Relate idea of parallel lines and transversal to streets on map of capital. <br> (Relate to a place they have interest in and motivate interest in lesson.) <br> May ask student to look up map of where they live and have them write directions to <br> get from their house to school. Need to include words from new vocabulary. |
| Language barrier | Review vocabulary, theorems, and symbols that are needed for the student to explain <br> their answers. (Specific needs of students should be met before lesson is presented.) <br> Vocabulary words are presented with pictures and symbols with consistent reference <br> to the spoken word, written word, and the visual representation. |
| Processing Comprehension | Differentiated instruction. Use masking tape to mark two parallel lines and a <br> transversal on the floor. Have pairs of students stand in angles that are congruent or |


|  | supplementary, and have them explain whether their angles are alternate interior, <br> alternate exterior, corresponding, or same-side angles. <br> Marking related lines and angles with colored markers. <br> Chunking the material. Direct instruction. Peer tutoring. Scaffolding. |
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| Organization | Post objective and agenda before class. Advance organizer available. Foldable. |
| ADD students | Preferential seating. Close proximity to teacher will aid student in staying on task. |


| Possible UDL Applications for Extension |  |  |  |  |  |  |
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| Representation | Some students may use the video "Figuring out angles between <br> transversal and parallel lines", at https://www.khanacademy.org. <br> Some students may watch power-point available on CD from <br> Glencoe McGraw-Hill textbook on identifying and finding measure <br> of angles formed by transversal and parallel lines. <br> All students have access to a TI-84 graphing calculator. Capri Jr. is <br> an apps on the calculator, very much like Geometer's Sketchpad. <br> The student could use the apps to find the measure of the angles and <br> the relationship between the angles. |  |  |  |  |  |
| Engagement | A Parallel Scavenger Hunt may be a way to motivate and engage <br> some students. The student should find as many examples of parallel <br> lines and planes in the following categories: Architecture, Art, Your |  |  |  |  |  |
| Home, Logos, Maps, Music and Musical Instruments, and nature. |  |  |  |  |  |  |
| You can use any reference materials you find helpful, including |  |  |  |  |  |  |
| books, encyclopedias, magazines, and the internet. |  |  |  |  |  |  |
| Use different colored markers to identify parallel lines and the |  |  |  |  |  |  |
| transversal. Use different colored makers to identify different types |  |  |  |  |  |  |
| of angles and congruent angles. |  |  |  |  |  |  |


|  | Mark off parallel lines on floor with masking tape. Have pairs of <br> students stand in angles that are congruent or supplementary. Have <br> them identify the types of angles and their relationship. <br> Another idea as suggested in the lesson critique, students could <br> make use of flip cameras and take pictures of parallel lines in their <br> world. |
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| Expression | Students take a pre and post-test to express their comprehension. <br> They will take a unit test after the unit on angles is completed. <br> The students may use the following alternative ways to illustrate <br> their comprehension. <br> All students have access to a TI-84 graphing calculator. Thus, the <br> student may choose to use the Capri Jr. apps on the calculator to <br> investigate angles formed by 2 parallel lines and a transversal. <br> Geometer's Sketchpad could also be used to assess the objective. <br> Student may use alternative assessment where they choose a <br> presentation website to show comprehensive of the objective. <br> The use of GeoGebra as an additional or alternative means of <br> expression was suggested in the critique. |

Level III: A few students will...write a two column proof or paragraph proof proving if two parallel lines are cut by a transversal, then each pair of corresponding angles are congruent.

Level II: Some students will...complete the proof of Corresponding Angles Postulate by writing the missing statements or reasons in a formal proof.

Level I: All students will...identify the relationship between two lines, classify angles formed by two lines and a transversal, and find their measures. The student will determine the relationship between angles formed by two parallel lines cut by a transversal.

## References:

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